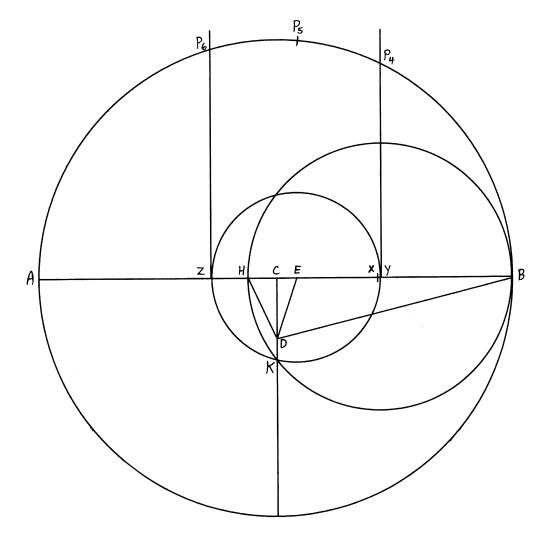
Construction of a 17-gon¹

- 1. Construct a circle with diameter AB and center C.
- 2. Construct a radius, perpendicular to AB, with point D on that radius such that $CD = \frac{1}{4} CA$.
- 3. Find point E on BC such that $\angle EDC = \frac{1}{4} \angle BDC$.
- 4. Find point H on AC such that \angle EDH is half a right angle (45°).
- 5. Draw a circle with BH as diameter, labeling its center as X and its intersection with line CD extended as K.
- 6. Draw a circle with E as its center and EK as its radius. Label this circle's intersection with BC as Y, and its intersection with AC as Z. (Note: X and Y are close, but do not actually coincide.)
- 7. Draw a line perpendicular to AB from Y and label where it crosses the original circle as P₄. Draw a line perpendicular to AB from Z and label where it crosses the original circle as P₆ (on the same side of AB as P₄).
- 8. Points P_4 and P_6 are the 4th and 6th vertices of the desired 17-gon. Find P_5 by bisecting $\angle P_4CP_6$.
- 9. Find the remaining vertices of the 17-gon by marking off the distance P_4P_5 around the perimeter of the circle. If done perfectly, point B will be the first vertex (P_1), and the radius CA bisects a side of the 17-gon.



¹ This particular construction is by H.W. Richmond (*Mathematische Annalen*, volume 67, 1909).
In 1796, Carl Friedrich Gauss proved that the 17-gon was constructible, but he did not provide a method for doing it. In 1800, Johannes Erchinger provided the first method for constructing the 17-gon.