

# Numbers as the Sum of Two Squares

(Numbers that are missing cannot be expressed as the sum of two squares.)

$$\mathbf{2} = 1^2 + 1^2$$

$$\mathbf{5} = 1^2 + 2^2$$

$$\mathbf{8} = 2^2 + 2^2$$

$$\mathbf{10} = 1^2 + 3^2$$

$$\mathbf{13} = 2^2 + 3^2$$

$$\mathbf{17} = 1^2 + 4^2$$

$$\mathbf{18} = 3^2 + 3^2$$

$$\mathbf{20} = 2^2 + 4^2$$

$$\mathbf{25} = 3^2 + 4^2$$

$$\mathbf{26} = 1^2 + 5^2$$

$$\mathbf{29} = 2^2 + 5^2$$

$$\mathbf{32} = 4^2 + 4^2$$

$$\mathbf{34} = 3^2 + 5^2$$

$$\mathbf{37} = 1^2 + 6^2$$

$$\mathbf{40} = 2^2 + 6^2$$

$$\mathbf{41} = 4^2 + 5^2$$

$$\mathbf{45} = 3^2 + 6^2$$

$$\mathbf{50} = 1^2 + 7^2; \quad 5^2 + 5^2$$

$$\mathbf{52} = 4^2 + 6^2$$

$$\mathbf{53} = 2^2 + 7^2$$

$$\mathbf{58} = 3^2 + 7^2$$

$$\mathbf{61} = 5^2 + 6^2$$

$$\mathbf{65} = 1^2 + 8^2; \quad 4^2 + 7^2$$

$$\mathbf{68} = 2^2 + 8^2$$

$$\mathbf{72} = 6^2 + 6^2$$

$$\mathbf{73} = 3^2 + 8^2$$

$$\mathbf{74} = 5^2 + 7^2$$

$$\mathbf{80} = 4^2 + 8^2$$

$$\mathbf{82} = 1^2 + 9^2$$

$$\mathbf{85} = 2^2 + 9^2; \quad 6^2 + 7^2$$

$$\mathbf{89} = 5^2 + 8^2$$

$$\mathbf{90} = 3^2 + 9^2$$

$$\mathbf{97} = 4^2 + 9^2$$

$$\mathbf{98} = 7^2 + 7^2$$

$$\mathbf{100} = 6^2 + 8^2$$

$$\mathbf{101} = 1^2 + 10^2$$

$$\mathbf{104} = 2^2 + 10^2$$

$$\mathbf{106} = 5^2 + 9^2$$

$$\mathbf{109} = 3^2 + 10^2$$

$$\mathbf{113} = 7^2 + 8^2$$

$$\mathbf{116} = 4^2 + 10^2$$

$$\mathbf{117} = 6^2 + 9^2$$

$$\mathbf{122} = 1^2 + 11^2$$

$$\mathbf{125} = 2^2 + 11^2; \quad 5^2 + 10^2$$

$$\mathbf{128} = 8^2 + 8^2$$

$$\mathbf{130} = 3^2 + 11^2; \quad 7^2 + 9^2$$

$$\mathbf{136} = 6^2 + 10^2$$

$$\mathbf{137} = 4^2 + 11^2$$

$$\mathbf{145} = 1^2 + 12^2; \quad 8^2 + 9^2$$

$$\mathbf{146} = 5^2 + 11^2$$

$$\mathbf{148} = 2^2 + 12^2$$

$$\mathbf{149} = 7^2 + 10^2$$

$$\mathbf{153} = 3^2 + 12^2$$

$$\mathbf{157} = 6^2 + 11^2$$

$$\mathbf{160} = 4^2 + 12^2$$

$$\mathbf{162} = 9^2 + 9^2$$

$$\mathbf{164} = 8^2 + 10^2$$

$$\mathbf{169} = 5^2 + 12^2$$

$$\mathbf{170} = 1^2 + 13^2; \quad 7^2 + 11^2$$

$$\mathbf{173} = 2^2 + 13^2$$

$$\mathbf{178} = 3^2 + 13^2$$

$$\mathbf{180} = 6^2 + 12^2$$

$$\mathbf{181} = 9^2 + 10^2$$

$$\mathbf{185} = 4^2 + 13^2; \quad 8^2 + 11^2$$

$$\mathbf{193} = 7^2 + 12^2$$

$$\mathbf{194} = 5^2 + 13^2$$

$$\mathbf{197} = 1^2 + 14^2$$

$$\mathbf{200} = 2^2 + 14^2; \quad 10^2 + 10^2$$

$$\mathbf{202} = 9^2 + 11^2$$

$$\mathbf{205} = 3^2 + 14^2; \quad 6^2 + 13^2$$

$$\mathbf{208} = 8^2 + 12^2$$

$$\mathbf{212} = 4^2 + 14^2$$

$$\mathbf{218} = 7^2 + 13^2$$

$$\mathbf{221} = 5^2 + 14^2; \quad 10^2 + 11^2$$

$$\mathbf{225} = 9^2 + 12^2$$

$$\mathbf{226} = 1^2 + 15^2$$

$$\mathbf{229} = 2^2 + 15^2$$

$$\mathbf{232} = 6^2 + 14^2$$

$$\mathbf{233} = 8^2 + 13^2$$

$$\mathbf{234} = 3^2 + 15^2$$

$$\mathbf{241} = 4^2 + 15^2$$

$$\mathbf{242} = 11^2 + 11^2$$

$$\mathbf{244} = 10^2 + 12^2$$

$$\mathbf{245} = 7^2 + 14^2$$

$$\mathbf{250} = 5^2 + 15^2; \quad 9^2 + 13^2$$

$$\mathbf{257} = 1^2 + 16^2$$

$$\mathbf{260} = 2^2 + 16^2; \quad 8^2 + 14^2$$

$$\mathbf{261} = 6^2 + 15^2$$

$$\mathbf{265} = 3^2 + 16^2; \quad 11^2 + 12^2$$

$$\mathbf{269} = 10^2 + 13^2$$

$$\mathbf{272} = 4^2 + 16^2$$

$$\mathbf{274} = 7^2 + 15^2$$

$$\mathbf{277} = 9^2 + 14^2$$

$$\mathbf{281} = 5^2 + 16^2$$

$$\mathbf{288} = 12^2 + 12^2$$

$$\mathbf{289} = 8^2 + 15^2$$

$$\mathbf{290} = 1^2 + 17^2; \quad 11^2 + 13^2$$

$$\mathbf{292} = 6^2 + 16^2$$

$$\mathbf{293} = 2^2 + 17^2$$

$$\mathbf{296} = 10^2 + 14^2$$

$$\mathbf{298} = 3^2 + 17^2$$

$$\mathbf{305} = 4^2 + 17^2; \quad 7^2 + 16^2$$

$$\mathbf{306} = 9^2 + 15^2$$

$$\mathbf{313} = 12^2 + 13^2$$

$$\mathbf{314} = 5^2 + 17^2$$

$$\mathbf{317} = 11^2 + 14^2$$

$$\mathbf{320} = 8^2 + 16^2$$

$$\mathbf{325} = 1^2 + 18^2; \quad 6^2 + 17^2; \quad 10^2 + 15^2$$

$$\mathbf{328} = 2^2 + 18^2$$

$$\mathbf{333} = 3^2 + 18^2$$

$$\mathbf{337} = 9^2 + 16^2$$

$$\mathbf{338} = 7^2 + 17^2; \quad 13^2 + 13^2$$

$$\mathbf{340} = 4^2 + 18^2; \quad 12^2 + 14^2$$

$$\mathbf{346} = 11^2 + 15^2$$

$$\mathbf{349} = 5^2 + 18^2$$

$$\mathbf{353} = 8^2 + 17^2$$

$$\mathbf{356} = 10^2 + 16^2$$

$$\mathbf{360} = 6^2 + 18^2$$

$$\mathbf{362} = 1^2 + 19^2$$

$$\mathbf{365} = 2^2 + 19^2; \quad 13^2 + 14^2$$

$$\mathbf{369} = 12^2 + 15^2$$

$$\mathbf{370} = 3^2 + 19^2; \quad 9^2 + 17^2$$

$$\mathbf{373} = 7^2 + 18^2$$

$$\mathbf{377} = 4^2 + 19^2; \quad 11^2 + 16^2$$

$$\mathbf{386} = 5^2 + 19^2$$

$$\mathbf{388} = 8^2 + 18^2$$

$$\mathbf{389} = 10^2 + 17^2$$

$$\mathbf{392} = 14^2 + 14^2$$

$$\mathbf{394} = 13^2 + 15^2$$

$$\mathbf{397} = 6^2 + 19^2$$

$$\mathbf{400} = 12^2 + 16^2$$

$$\mathbf{401} = 1^2 + 20^2$$

$$\mathbf{404} = 2^2 + 20^2$$

$$\mathbf{405} = 9^2 + 18^2$$

$$\mathbf{409} = 3^2 + 20^2$$

$$\mathbf{410} = 7^2 + 19^2; \quad 11^2 + 17^2$$

$$\mathbf{416} = 4^2 + 20^2$$

$$\mathbf{421} = 14^2 + 15^2$$

$$\mathbf{424} = 10^2 + 18^2$$

$$\mathbf{425} = 5^2 + 20^2; \quad 8^2 + 19^2; \quad 13^2 + 16^2$$

$$\mathbf{433} = 12^2 + 17^2$$

$$\mathbf{436} = 6^2 + 20^2$$

$$\mathbf{442} = 1^2 + 21^2; \quad 9^2 + 19^2$$

The first number that can be

expressed in 4 ways is...

$$\mathbf{1105} = 4^2 + 33^2; \quad 9^2 + 32^2;$$

$$12^2 + 31^2; \quad 23^2 + 24^2$$