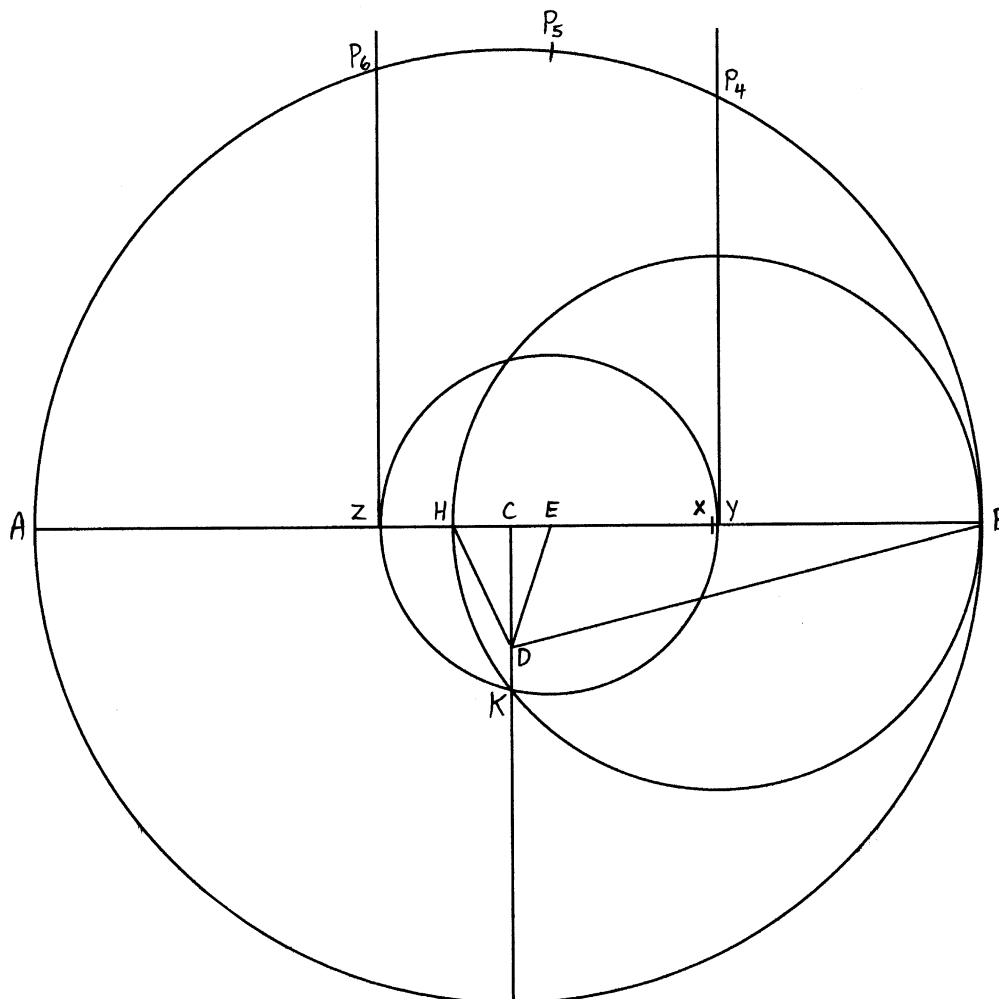


# Construction of a 17-gon<sup>1</sup>

1. Construct a circle with diameter AB and center C.
2. Construct a radius, perpendicular to AB, with point D on that radius such that  $CD = \frac{1}{4} CA$ .
3. Find point E on BC such that  $\angle EDC = \frac{1}{4} \angle BDC$ .
4. Find point H on AC such that  $\angle EDH$  is half a right angle ( $45^\circ$ ).
5. Draw a circle with BH as diameter, labeling its center as X and its intersection with line CD extended as K.
6. Draw a circle with E as its center and EK as its radius. Label this circle's intersection with BC as Y, and its intersection with AC as Z. (Note: X and Y are close, but do not actually coincide.)
7. Draw a line perpendicular to AB from Y and label where it crosses the original circle as  $P_4$ .  
Draw a line perpendicular to AB from Z and label where it crosses the original circle as  $P_6$  (on the same side of AB as  $P_4$ ).
8. Points  $P_4$  and  $P_6$  are the 4<sup>th</sup> and 6<sup>th</sup> vertices of the desired 17-gon. Find  $P_5$  by bisecting  $\angle P_4CP_6$ .
9. Find the remaining vertices of the 17-gon by marking off the distance  $P_4P_5$  around the perimeter of the circle. If done perfectly, point B will be the first vertex ( $P_1$ ), and the radius CA bisects a side of the 17-gon.



<sup>1</sup> This particular construction is by H.W. Richmond (*Mathematische Annalen*, volume 67, 1909).

In 1796, Carl Friedrich Gauss proved that the 17-gon was constructible, but he did not provide a method for doing it. In 1800, Johannes Erchinger provided the first method for constructing the 17-gon.